

**TITLE OF THE INVENTION**

**METHOD AND APPARATUS FOR MEASURING REVENUE  
PERFORMANCE FOR A LODGING ESTABLISHMENT**

**BACKGROUND OF THE INVENTION**

**5     Field of the Invention**

The invention relates to measuring financial performance in general and more particularly to a method and apparatus for measuring the financial performance of an entity for a given demand.

**Background**

10           The hospitality industry is extremely competitive. In order to succeed in the hospitality industry, proper management of available resources is important. Available resources in the hospitality industry include rooms in which guests sleep and function space (e.g., ballrooms, meeting rooms, etc.) used by guests for other purposes. It is common in the hospitality industry to classify consumers of these  
15           resources as belonging to one of two types: transient and group. Transient consumers are those consumers who need a single room or a small number of rooms in which to sleep for a period of time, but who do not utilize function space. Group consumers are those consumers who need a large number of rooms. Group consumers also typically, but not necessarily, require function space.

20           Where the demand for resources is less than the supply (i.e., occupancy is low), resource management is simple - all demands (i.e., requests for rooms and/or

function space) are accepted (i.e., rooms and function space are sold to all customers who ask for it). The more difficult management problem occurs when demand, or expected demand, exceeds supply. In this situation, effectively managing resources requires decisions as to which demands (requests) for rooms and function space to accept and which to refuse.

Further complicating the management issue is the existence of different rates for the same room. A hospitality establishment such as a hotel often has an established “rack rate” at which it will rent a given room to a single person with little or no advance registration. The same room will often be rented to a person who is part of a group at a different, lower rate, and may be rented at yet another promotional rate at different times.

Additionally, hospitality establishments often enter into arrangements with resellers such as tour operators under which the reseller agrees to fill a large volume of rooms from the hospitality establishment in return for a discounted rate. Under such agreements, the hospitality establishment often must provide a room to such resellers whenever the room is requested, even if the hospitality establishment believes there will be a demand for the room (i.e., an opportunity to rent the room) from higher paying customers (this is sometimes referred to as last room availability).

As a practical matter, it is necessary to make management decisions as to whether to dedicate a resource (i.e., confirm a reservation) when the demand is made. This means, for example, that a hotel with 15 available rooms for an upcoming weekend must make a decision on a group demand for 10 rooms not

knowing whether other demands (which may be transient or group demands) for some or all of those rooms will occur after the group demand is received.

Some attempts at implementing rules and procedures for responding to (i.e., deciding whether to accept or reject) these demands have been made. These rules and procedures are commonly referred to as “revenue management controls,”  
5 “revenue optimization techniques,” or “yield management.” The effectiveness of these revenue management controls can be measured in a number of ways. One possible way of measuring the effectiveness is by comparing the actual occupancy rate with the theoretical maximum occupancy rate for a given demand. However,  
10 this measurement technique ignores the aforementioned difference in room rates. A more effective measurement technique is to measure effectiveness by comparing an amount of revenue or profit actually realized as a function of total revenue or profit that could have been realized for a given demand amount had the optimal decisions on whether to accept or deny a demand been made.

15 Typical management effectiveness measurement techniques in the hospitality industry are concerned only with the transient portion of the management problem. For example, some existing techniques completely ignore revenue and profit from function space and simply subtract rooms rented to group guests from the “inventory” of available rooms for which management  
20 effectiveness is measured.

What is needed is a method and apparatus that measures the management effectiveness for both function and room space for both group and transient customers.

## **BRIEF SUMMARY OF THE INVENTION**

The present invention addresses the aforementioned issues to a great extent by providing methods and apparatuses for calculating an optimal total yield, which may be revenue or profit, for both individual space (e.g., sleeping rooms) and function space (e.g., ballrooms) in an entity (e.g., a hospitality establishment) for a set of demands that includes both group and transient demands. In a preferred embodiment of the invention, the optimization problem is characterized as a mixed-integer linear programming (MILP) problem and solved using MILP techniques. In some embodiments, a small value is assigned to the “cost” of a room upgrade and the cost of room upgrades are included in the revenue or profit function to be optimized. In some embodiments of the invention, the actual revenue or profit yield is compared to the optimum revenue or profit yield.

## **BRIEF DESCRIPTION OF THE FIGURES**

A more complete appreciation of the invention and many of the attendant features and advantages thereof will be readily obtained as the same become better understood by reference to the following detailed description when considered in connection with the accompanying drawings, wherein:

Figure 1 is a block diagram representing configurable function space in an exemplary hotel.

Figure 2 is flowchart illustrating an overview of the method, according to one embodiment of the present invention.

Figure 3 is a flowchart illustrating various constraints and how the various constraints are determined.

Figure 4 is a flowchart illustrating various bounds and how the various bounds are determined.

### **DETAILED DESCRIPTION**

The present invention will be discussed with reference to preferred  
5      embodiments of methods and apparatuses for calculating an optimal revenue or  
profit for a hospitality establishment for a given demand set. Specific details are  
set forth in order to provide a thorough understanding of the present invention.  
The preferred embodiments discussed herein should not be understood to limit the  
invention. Furthermore, for ease of understanding, certain method steps are  
10     delineated as separate steps; however, these steps should not be construed as  
necessarily distinct nor order dependent in their performance.

As used herein, a “demand” is request for a room or function space.  
Demands may be made, for example, by customers who literally walk up to a front  
desk at a lodging establishment or by customers who make a telephone call to the  
15     individual lodging establishment or to a nationwide reservation system, or over the  
Internet. Demands are recorded as they are received whether or not they are  
accepted (i.e., whether or not a sleeping room or function space is rented to the  
customer making the demand). In the preferred embodiments discussed below, the  
demands from individual transient customers are aggregated into a four  
20     dimensional array of a number of demands for each arrival date (AD), length of  
stay (LS), rate category (RC), and room type (RT). In contrast, the group demands  
are not aggregated but rather are treated separately. As will be discussed in further  
detail below, the preferred embodiments allow any number of transient demands

for a given arrival date, length of stay, rate category and room type to be accepted. That is, none, one, some, or all of the demands for a given AD, LS, RC and RT may be accepted in order to optimize profit. This reflects the fact that transient demands, unlike group demands, are usually received for one room at a time.

5 Group demands are not separable and must be accepted or rejected in their entirety.

It should also be noted that preferred embodiments of the invention decide which demands to accept or reject without consideration of whether the demands are made by resellers from whom the hospitality establishment is contractually obligated to accept demands. In this way, the difference between the optimal yield  
10 and the actual yield will reflect some of the “cost” (i.e., the difference between what revenue or profit was actually received as a result of allocating the room to a demand by the reseller pursuant to a contractual arrangement rather than allocating the room to a transient demand at a higher rate) of the arrangement with the reseller to be determined.

15 The preferred embodiments discussed herein will be illustrated in the context of a fictional hotel and a fictional set of transient and group demands for a three day period (days 0, 1, and 2). In practice, the usual period is one month. The fictional hotel has 20 each of three types of rooms designated as room types (RT) 0, 1, and 2. Room type 0 is the smallest and least desirable, and room type 2 is the  
20 largest and most desirable. On any given night, not all rooms may be available. A room might not be available due to, for example, a leaking pipe in the room or renovations being done to the room. Table 5 lists the availability of the various rooms in the fictional hotel for the fictional three day period of the example.

The fictional hotel has three function space areas: two ballrooms referred to as BALL1 and BALL2, and an outdoor patio near the pool referred to as POOL. The POOL space cannot be sub-divided into smaller function spaces. However, each of the ballrooms BALL1 and BALL2 includes two folding, retractable walls which allow the ballrooms to be divided into smaller, function spaces (the smallest function spaces, which cannot be further divided, are referred herein as indivisible specific spaces). This is illustrated diagrammatically in Fig. 1. Ballroom 100 BALL1 has two walls 110,120. When both walls 110,120 are extended, BALL1 is divided into three indivisible specific spaces (sometimes referred to as salons) A1, B1, C1. If wall 110 is extended and wall 120 is retracted, BALL1 is divided into salon A1 and meeting room BC1 (BC1 is the combination of function spaces B1 and C1). Conversely, if wall 110 is retracted and wall 120 is extended, BALL1 is divided into meeting room AB1 and salon C1. Ballroom 200 BALL2 is similarly configurable into function spaces A2, B2, C2, AB2 and BC2 through the selective extension and retraction of walls 210, 220. Table 9 illustrates the square footage of each of the various function spaces for our fictional hotel. As illustrated in Table 9, these function spaces are assigned a function space category (also referred to herein as target space type or TST) of 0-7 depending on their square footage, with the smallest spaces assigned a space category/TST of 0 and the highest assigned a space category/TST of 7. It will be assumed that two function spaces with the same square footage/space category are interchangeable (e.g., a group demand for a target space type or space category 3=300 sq. ft. can be satisfied by function space C2 or BC1), and that a demand for any smaller function space can be filled with any larger function space (e.g., a demand for a 300 square foot function space can

be filled with a function space with a space category of 3=300 sq. ft. or any other function space with a larger square footage (a space code greater than 3). Table 7 lists the various TSTs for the hotel.

5 A set of fictional transient sleeping room demands for our fictional hotel is listed in Table 6, and a set of group demands (which are sometimes referred to herein as “opportunities” and which include both sleeping room and function space components) is set forth in Tables 11-13. As shown therein, the fictional example includes three group demands with identifiers (OID) of “ATT,” “IBM,” and “CSCO.”

10 Figure 2 is flowchart illustrating an overview of a method for calculating an optimal yield according to one embodiment of the present invention. The yield may be either revenue or profit. The method illustrated in Figure 2 calculates an optimal total yield for both sleeping rooms and function space in a hospitality establishment for a demand set including both transient and group demands. In  
15 step 205, a yield formula that includes yield from both individual space (i.e., sleeping room) and function space for both transient and group demands is set. In step 210, constraints under which the yield is optimized are determined. As used herein, a “constraint” is a condition that impacts the optimum yield. In step 215, bounds for the revenue optimization problem are determined. In step 220, the  
20 optimal total yield problem formulated in steps 205, 210 and 215 is solved utilizing mixed-integer linear programming (MILP) techniques.



### **Set Yield Equation**

In preferred embodiments of the invention, determining an optimum yield given a set of demands is preferably formulated as a mixed integer linear programming problem. The objective of the problem is to maximize the yield (which may be revenue or profit) from both the sleeping space and the function space of a hospitality establishment for both group and transient guests. The following example will be illustrated in terms of revenue but it should be understood that profit may be substituted for revenue in the following equations.

The total revenue R is defined as:

$$R = \text{TrRev} - 0.001\text{UpCst} + \text{GrRev}$$

where TrRev is the revenue associated with all accepted transient demand, GrRev is the revenue associated with all acceptable group demand, and UpCst adds a penalty for upgrading sleeping rooms.

### **Determine Constraints**

Figure 3 is a flowchart illustrating various constraints and how the various constraints are determined. The first three constraints are essentially definitions of the three components of the revenue formula described above.

In step 305, the transient revenue TrRev constraint TrRevDef is set, defining the revenue for the transient rooms that have been accepted by taking the cost of each accepted room into account.

$$-\sum_i R(i)x. AD(i). LS(I). RC(i). RT(i) + TrRev = 0$$

Or written another way:

$$TrRev = \sum_i R(i) \cdot x \cdot AD(i) \cdot LS(i) \cdot RC(i) \cdot Rt(i)$$

where  $i$  is a transient demand,  $x(i).AD(i).LS(i).RC(i).RT(i)$  is an integer value representing the number of demands  $i$  for a corresponding AD, LS, RC and RT that are accepted, and  $R(i)$  is the revenue associated with the demand  $i$ . As discussed above, the aggregated demands  $i$  preferably take the form of a four dimensional  
5 array, where the indices are arrival date (AD), length of stay (LS) (a length of stay of 0 represents one night), rate category (RC), and room type (RT) and the values in the array represent the number of sleeping rooms demanded for the corresponding indices. The arrival date (AD) and length of stay (LS) are self explanatory. The rate category (RC) corresponds to a dollar amount associated  
10 with each day the room is rented. The room type (RT) refers to the size and type of room (e.g., single room, suite).

There is a separate  $x$  variable for each demand record as indicated in Table 2.  $I$  in Table 2 represents the total number of demand records. It should be understood that the total number of demand records  $I$  may be less than the total  
15 number of possible combinations of AD, LS, RC and RT because a demand for a particular combination of AD, LS, RC and RT may not have been received in a particular period of interest.

In our fictional example, the transient revenue  $TrRev$  is calculated, using the four transient demands listed in Table 6, as follows:

$$TrRev = (300 \cdot x \cdot 0.2 \cdot 0.0) + (100 \cdot x \cdot 1.0 \cdot 0.1) + (120 \cdot x \cdot 2.0 \cdot 1.1) + (150 \cdot x \cdot 2.0 \cdot 2.2)$$

Note that there are four x variables (x.0.2.0.0, x.1.0.0.1, x.2.0.1.1, and x.2.0.2.2), one for each of the four transient demands listed in Table 6. The coefficients R(i) of the four x variables are obtained by multiplying the room rate from Table 6 by the length of stay LS. Thus, for example, in the first value, the room rate is 100 per night, with a length of stay (LS) of 2 (meaning three nights), so the revenue for three nights at 100 per night is 300.

In step 310, the upgrade cost constraint UpCst Def is set. The upgrade cost UpCst is an integer value that represents the number of times a transient guest is upgraded to a better (e.g., more expensive) sleeping room at no cost to the customer. By multiplying UpCst by -.0001 (or any other small constant) in the revenue equation, a small “cost” is assigned to room upgrades. This is done to ensure that the model will not unnecessarily assign upgraded sleeping rooms for transient demands that are accepted. The constraint is:

$$-\sum_i \sum_{ART > RT(i)} y \cdot AD(i) \cdot LS(i) \cdot RC(i) \cdot RT(i) \cdot ART + UpCst = 0$$

Or written another way:

$$UpCst = \sum_i \sum_{ART > RT(i)} y \cdot AD(i) \cdot LS(i) \cdot RC(i) \cdot RT(i) \cdot ART$$

where y.AD(i).LS(i).RC(i).RT(i).ART are the room allocation variables that represent the number of rooms of allocated room type ART that are allocated to each transient demand i for room type RT. Thus, for each x variable, there is a list of y variables associated with room types that can be allocated to fill the demand i, which must be as good or better than the type of room in the demand i.

Thus, the total number of y variables is  $\sum_i (NRT - RT(i) + 1)$ , where NRT is the number of room types in the lodging establishment (3 in the fictional example) and RT(i) is the room type associated with demand i. The upgrade cost UpCst is thus calculated by looking at each demand itinerary i, and adding up the transient rooms that were assigned an upgrade (e.g., where ART > RT(i)).

Using the example demands in Table 6, and assigned room type (ART) values where ART > RT(i) (e.g., thus, if RT is 0, ART is 1 and 2), the upgrade cost UpCst is calculated as follows:

$$UpCst = y_{0.2.0.0.1} + y_{0.2.0.0.2} + y_{1.0.0.1.2} + y_{2.0.1.1.2}$$

In step 315, the group revenue GrRev constraint GrRevDef is set. This constraint defines the group revenue GrRev portion of the revenue equation. The group revenue constraint GrRevDef is:

$$- \sum_{OID} R(OID)w_{Opp.OID} + GrRev = 0$$

Or written another way:

$$GrRev = \sum_{OID} R(OID)w_{Opp.OID}$$

where w.Opp.OID is a binary value representing whether or not a group demand (or opportunity) was accepted (if the opportunity OID is accepted, w.Opp.OID is equal to 1, if the opportunity was turned down, w.Opp.OID is equal to 0); and R(OID) is the revenue associated with the group demand. As set forth in Table 2, there are NOID of these binary variables, where NOID represents the number of group demands. Unlike the transient demands i, the group demands OID are not aggregated and, because of their nature as a group demand, must be accepted or

rejected in their entirety - hence the binary value  $w_{Opp.OID}$  associated with each group demand. The group demands OID include both a function space component and a sleeping room component as discussed above.

5      Using the example values from Table 11 for  $R(OID)$ , the group revenue is calculated as:

$$GrRev = 2001w_{Opp.ATT} + 2002w_{Opp.CSCO} + 2000w_{Opp.IBM}$$

In step 320, an upper bound constraint  $x_{UbCon.i}$  is set for each demand  $i$ . This constraint represents an upper bound on the number of sleeping rooms that the model can allocate to a transient demand (e.g., if there are 100 rooms in an aggregated demand  $i$  for a given AD, LS, RC and RT, the model cannot allocate  
10      more than 100 rooms to that demand  $i$ ). The upper bound constraint  $x_{UbCon.i}$  is:

$$x_{UbCon.i}: x.AD(i).LS(i).RC(i).RT(i) \leq N(i) \quad \forall i$$

where  $x.AD(i)$ ,  $LS(i)$ ,  $RC(i)$ , and  $RT(i)$  are as previously described and  $N(i)$  represents the number of sleeping rooms for demand  $i$ .  $\forall i$  signifies “for all  $i$ ”.

Using the demand information in Table 6, the four upper bound constraints  
15       $x_{UbCon.i}$  for each of the four demands  $i$  in the fictional example are as follows:

$$x_{UbCon.0.Def}: x.0.2.0.0 \leq 3$$

$$x_{UbCon.1.Def}: x.1.0.0.1 \leq 4$$

$$x_{UbCon.2.Def}: x.2.0.1.1 \leq 5$$

$$x_{UbCon.3.Def}: x.2.0.2.2 \leq 6$$

In step 325, the transient upgrade and allocation constraints  $TrUpd.AD(i).LS(i).RC(i).RT(i)$  for each of the demands  $i$  are set. These

constraints ensure that customers are assigned to a room at least as “good” as the room type they requested (e.g., if someone requested room type 1, they would be assigned room type 1 or 2, but would not be downgraded to inferior room type 0).

Thus:

$$\begin{aligned} & \text{TrUpg.AD(i).LS(i).RC(i).RT(i).Def:} \\ & -x.\text{AD(i).LS(i).RC(i).RT(i)} + \sum_{\text{ART} \geq \text{RT(i)}} y.\text{AD(i).LS(i).RC(i).RT(i).ART} \geq 0 \quad \forall i \end{aligned}$$

5 Or written another way:

$$\sum_{\text{ART} \geq \text{RT(i)}} y.\text{AD(i).LS(i).RC(i).RT(i).ART} \geq x.\text{AD(i).LS(i).RC(i).Rt(i)} \quad \forall i$$

where  $x.\text{AD(i).LS(i).RC(i).RT(i)}$  and  $y.\text{AD(i).LS(i).RC(i).RT(i).ART}$  are as described above. To ensure customers are not being downgraded, this constraint requires the assigned room type (ART) to be greater than or equal to the room type (RT). For example, when the room type RT is 0, the allowable values for the ART are 0, 1, 2; when the RT is 1, the allowable values for ART are 1, 2; and when the RT is 2, the only allowable value for ART is 2.

Using the example values in Table 6, we get the following constraints.

$$\begin{aligned} & \text{TrUpg.0.2.0.0.Def: } -x.0.2.0.0 + y.0.2.0.0.0 + y.0.2.0.0.1 + y.0.2.0.0.2 \geq 0 \\ & \text{TrUpg.1.0.0.1.Def: } -x.1.0.0.1 + y.1.0.0.1.1 + y.1.0.0.1.2 \geq 0 \\ & \text{TrUpg.2.0.1.1.Def: } -x.2.0.1.1 + y.2.0.1.1.1 + y.2.0.1.1.2 \geq 0 \\ & \text{TrUpg.2.0.2.2.Def: } -x.2.0.0.2 + y.2.0.2.2.2 \geq 0 \end{aligned}$$

In step 330, the room protection  $\text{RmPr.SD.RT.Def}$  constraints are set.

These constraints define the total number of assigned sleeping rooms of a given room type that are allocated to transient and group demands. As will be discussed

below, these constraints are used together with a boundary condition to ensure that the total number of sleeping rooms of a given type allocated to transient and group demands do not exceed the total amount of hotel sleeping rooms of that room type that are available for a given day. In other words, these constraints ensure that the model cannot accept more demands for sleeping rooms than the hospitality establishment can accommodate. The room protection constraints are as follows

RmPr.SD.RTDef:

$$10 \quad \sum_{i | AD(i) \leq SD(i), AD(i) + LS(i) \geq SD, ART = RT} y.AD(i).LS(i).RC(i).RT(i).ART + \sum_{OID} \sum_{rt | ART(rt) = RT} yOpp.OID.SD.RT.ART(RT)] - RmPr(SD, RT) \leq 0$$

There is a room protection constraint RmPr.SD.RT for each stay date (SD) and room type (RT). Thus, as shown in Table 2, there are NSD \* NRT such RmPr constraints, where NSD is the number of stay dates (usually 28 but in our example, 3 (0, 1, and 2)), and NRT is the number of room types (3 in our example). The variables y.AD(i).LS(i).RC(i).RT(i).ART and x.AD(i).LS(i).RC(i).RT(i) are as described above. The summation for these variables is taken for all i where all three of the following conditions are met: (i) the arrival date must be before or on the stay date in question (i.e., AD(i) ≤ SD(i)), (ii) the arrival date plus the length of stay must be greater than or equal to the stay date in question (i.e., AD(i) + LS(i) ≥ SD), and the assigned room type must be equal to the room type in question (i.e., ART = RT). The group sleeping room allocation variables yOpp.OID.SD.RT.ART represent the number of rooms of allocated room type ART

that are allocated to fill each accepted group demand OID for a room type RT. The summation for these variables is taken for room types where the assigned room type (ART) is equal to the room type (RT) corresponding to the constraint, for all opportunity IDs (OID).

5           Using example stay dates (SD) and room types (RT) from Table 5, the transient demand information from Table 6, and the group demand sleeping room information from Table 12, the RmPr constraints are as follows:

$$\begin{aligned}
 &\text{RmPr.0.0.Def: } y_{0.2.0.0.0} + y_{\text{Opp.ATT.0.0.0}} + y_{\text{Opp.CSCO.0.0.0}} + y_{\text{Opp.IBM.0.0.0}} - \text{RmPr.0.0} \leq 0 \\
 &\text{RmPr.0.1.Def: } y_{0.2.0.0.1} + y_{\text{Opp.ATT.0.0.1}} + y_{\text{Opp.CSCO.0.0.1}} + y_{\text{Opp.IBM.0.0.1}} - \text{RmPr.0.1} \leq 0 \\
 10 \quad &\text{RmPr.0.2.Def: } y_{0.2.0.0.2} + y_{\text{Opp.ATT.0.0.2}} + y_{\text{Opp.CSCO.0.0.2}} + y_{\text{Opp.IBM.0.0.2}} - \text{RmPr.0.2} \leq 0 \\
 &\text{RmPr.1.0.Def: } y_{0.2.0.0.0} - \text{RmPr.1.0} \leq 0 \\
 &\text{RmPr.1.1.Def: } y_{0.2.0.0.1} + y_{1.0.0.1.1} + y_{\text{Opp.ATT.1.1.1}} + y_{\text{Opp.IBM.1.1.1}} - \text{RmPr.1.1} = 0 \\
 &\text{RmPr.1.2.Def: } y_{0.2.0.0.2} + y_{1.0.0.1.2} + y_{\text{Opp.ATT.1.1.2}} + y_{\text{Opp.IBM.1.1.2}} - \text{RmPr.1.2} = 0 \\
 &\text{RmPr.2.0.Def: } y_{0.2.0.0.0} - \text{RmPr.2.0} \\
 15 \quad &\text{RmPr.2.1.Def: } y_{0.2.0.0.1} + y_{2.0.0.1.1} - \text{RmPr.2.1} \leq 0 \\
 &\text{RmPr.2.2.Def: } y_{0.2.0.0.2} + y_{2.0.0.1.2} + y_{2.0.0.2.2} - \text{RmPr.2.2} \leq 0
 \end{aligned}$$

In step 335, the group sleeping room constraint GpRmPr.OID.SD.RT.Def is set, ensuring that the sleeping room demand for a given group demand/opportunity is fully satisfied (e.g., if a group demand/opportunity is accepted, everyone in the group must be given a sleeping room). For each group demand/opportunity, there is a separate group sleeping room constraint for each stay date and room type on which a sleeping room is requested in the group demand/opportunity. The form of the group sleeping room constraints is:

$$25 \quad \text{GpRmPr.OID.SD.RT.Def: } \sum_{\text{ART} \geq \text{RT}} y_{\text{Opp.OID.SD.RT.ART}} - N(\text{OID}, \text{SD}, \text{RT}) w_{\text{Opp.OID}} \geq 0$$

Or written another way:

$$\sum_{\text{ART} \geq \text{RT}} y_{\text{Opp.OID.SD.RT.ART}} \geq N(\text{OID}, \text{SD}, \text{RT}) w_{\text{Opp.OID}}$$



The variables yOpp.OID.SD.RT.ART and wOpp.OID were described above. N(OID, SD, RT) represents the number of sleeping rooms associated with demand/opportunity OID for stay date DS and room type RT.

Using the values of SD, RT, and OID from Table 12, and  $ART \geq RT$ :

- 5 GpRmPr.ATT.0.0.Def:  $yOpp.ATT.0.0.0 + yOpp.ATT.0.0.1 + yOpp.ATT.0.0.2 - 4wOpp.ATT \geq 0$ .  
 GpRmPr.ATT.1.1.Def:  $yOpp.ATT.1.1.1 + yOpp.ATT.1.1.2 - 8wOpp.ATT \geq 0$   
 GpRmPr.CSCO.0.0.Def:  $yOpp.CSCO.0.0.0 + yOpp.CSCO.0.0.1 + yOpp.CSCO.0.0.2 - 5wOpp.CSCO \geq 0$   
 10 GpRmPr.IBM.0.0.Def:  $yOpp.IBM.0.0.0 + yOpp.IBM.0.0.1 + yOpp.IBM.0.0.2 - 3wOpp.IBM \geq 0$   
 GpRmPr.IBM.1.1.Def:  $yOpp.IBM.1.1.1 + yOpp.IBM.1.1.2 - 7wOpp.IBM \geq 0$

In step 340, the space constraints spc.DP.SS.Def are determined. The spc.DP.SS.Def constraints ensure that the same function space is not used more than once during a given day part. The spc.DP.SS constraints are defined as:

15 
$$spc.DP.SS.Def: \sum_{SS \in C(SS)} sscfu.DP.SS \leq 1 \quad \forall SS, DP$$

Or written another way:

$$\sum_{SS \in C(SS)} sscfu.DP.SS \leq 1 \quad \forall SS, DP$$

20 sscfu.DP.SS. represents whether indivisible specific space (SS) is being used during a specific day part (DP), for all specific space types (SST) and day parts (DP). C(SS) represents a set of all spaces that conflict with space SS. (I.e., given the following indivisible specific space A, B, C with basic configurations AB, BC, ABC here is a list of all sets.  $C(A) = \{A, AB, ABC\}$ ;  $C(B) = \{B, AB, BC, ABC\}$ ;  $C(C) = \{C, BC, ABC\}$ .)

25 In the example below, the day part is 0, 1, 2, or 3 (each representing 6 hours: thus day part (DP) 0 represents 12AM - 6 AM; day part (DP) 1 represents 6

AM to 12 PM; day part (DP) 2 represents 12 PM to 6 PM; day part (DP) 3 represents 6 PM to 12 PM). SS is the indivisible specific space (space code), as shown in Table 9. Thus:

$$\begin{aligned}
& \text{spc.0.A1.Def: } \text{sscfu.0.A1} + \text{sscfu.0.AB1} + \text{sscfu.0.BALL1} \leq 1 \\
& \text{spc.0.A2.Def: } \text{sscfu.0.A2} + \text{sscfu.0.AB2} + \text{sscfu.0.BALL2} \leq 1 \\
& \text{spc.0.B1.Def: } \text{sscfu.0.AB1} + \text{sscfu.0.BALL1} + \text{sscfu.0.B1} + \text{sscfu.0.BC1} \leq 1 \\
& \text{spc.0.B2.Def: } \text{sscfu.0.AB2} + \text{sscfu.0.BALL2} + \text{sscfu.0.B2} + \text{sscfu.0.BC2} \leq 1 \\
& \text{spc.0.C1.Def: } \text{sscfu.0.BALL1} + \text{sscfu.0.BC1} + \text{sscfu.0.C1} \leq 1 \\
& \text{spc.0.C2.Def: } \text{sscfu.0.BALL2} + \text{sscfu.0.BC2} + \text{sscfu.0.C2} \leq 1 \\
& \text{spc.1.A1.Def: } \text{sscfu.1.A1} + \text{sscfu.1.AB1} + \text{sscfu.1.BALL1} \leq 1 \\
& \text{spc.1.A2.Def: } \text{sscfu.1.A2} + \text{sscfu.1.AB2} + \text{sscfu.1.BALL2} \leq 1 \\
& \text{spc.1.B1.Def: } \text{sscfu.1.AB1} + \text{sscfu.1.BALL1} + \text{sscfu.1.B1} + \text{sscfu.1.BC1} \leq 1 \\
& \text{spc.1.B2.Def: } \text{sscfu.1.AB2} + \text{sscfu.1.BALL2} + \text{sscfu.1.B2} + \text{sscfu.1.BC2} \leq 1 \\
& \text{spc.1.C1.Def: } \text{sscfu.1.BALL1} + \text{sscfu.1.BC1} + \text{sscfu.1.C1} \leq 1 \\
& \text{spc.1.C2.Def: } \text{sscfu.1.BALL2} + \text{sscfu.1.BC2} + \text{sscfu.1.C2} \leq 1 \\
& \text{spc.2.A1.Def: } \text{sscfu.2.A1} + \text{sscfu.2.AB1} + \text{sscfu.2.BALL1} \leq 1 \\
& \text{spc.2.A2.Def: } \text{sscfu.2.A2} + \text{sscfu.2.AB2} + \text{sscfu.2.BALL2} \leq 1 \\
& \text{spc.2.B1.Def: } \text{sscfu.2.AB1} + \text{sscfu.2.BALL1} + \text{sscfu.2.B1} + \text{sscfu.2.BC1} \leq 1 \\
& \text{spc.2.B2.Def: } \text{sscfu.2.AB2} + \text{sscfu.2.BALL2} + \text{sscfu.2.B2} + \text{sscfu.2.BC2} \leq 1 \\
& \text{spc.2.C1.Def: } \text{sscfu.2.BALL1} + \text{sscfu.2.BC1} + \text{sscfu.2.C1} \leq 1 \\
& \text{spc.2.C2.Def: } \text{sscfu.2.BALL2} + \text{sscfu.2.BC2} + \text{sscfu.2.C2} \leq 1 \\
& \text{spc.3.A1.Def: } \text{sscfu.3.A1} + \text{sscfu.3.AB1} + \text{sscfu.3.BALL1} \leq 1 \\
& \text{spc.3.A2.Def: } \text{sscfu.3.A2} + \text{sscfu.3.AB2} + \text{sscfu.3.BALL2} \leq 1 \\
& \text{spc.3.B1.Def: } \text{sscfu.3.AB1} + \text{sscfu.3.BALL1} + \text{sscfu.3.B1} + \text{sscfu.3.BC1} \leq 1 \\
& \text{spc.3.B2.Def: } \text{sscfu.3.AB2} + \text{sscfu.3.BALL2} + \text{sscfu.3.B2} + \text{sscfu.3.BC2} \leq 1 \\
& \text{spc.3.C1.Def: } \text{sscfu.3.BALL1} + \text{sscfu.3.BC1} + \text{sscfu.3.C1} \leq 1 \\
& \text{spc.3.C2.Def: } \text{sscfu.3.BALL2} + \text{sscfu.3.BC2} + \text{sscfu.3.C2} \leq 1
\end{aligned}$$

In step 345, the assigned function space constraints tsa.DP.TST.Def are determined. The target space availability (tsa) variables tsa.DP.TST express the indivisible space usage, and the assigned function space constraints tsa.DP.TST.Def ensure that the area of the function space(s) assigned to a group demand for a function space is at least as great as the amount of function space area requested. The assigned function space constraints are defined as:

$$\text{tsa.DP.TST.Def: } \sum_{SS \in C(\text{TST})} \text{sscfu.DP.SS} - \text{tsa.DP.TST} = 0 \quad \forall \text{TST, DP}$$

Or written another way:

$$\text{tsa.DP.TST} = \sum_{SS \in C(\text{TST})} \text{sscfu.DP.SS}$$

tsa.DP.TST represents the target space available of a given target space type (target space type is also referred to as function space category). There are NDP X NTST such variables. NDP represents the number of day parts. NTST represents the number of target space types.

sscfu.DP.SS represents whether indivisible specific space SS is being used during day part P. SS is the indivisible specific space (space code), as shown in Table 9. TST is the target space type (space category) from Table 9. SS(TST) is the set of all indivisible specific spaces that produce the given target space type. DP is the day part and is 0, 1, 2, or 3 (each representing 6 hours as described above). Thus:

$$\begin{aligned} \text{tsa.0.0.Def: } & \text{sscfu.0.A1} + \text{sscfu.0.A2} + \text{sscfu.0.B1} - \text{tsa.0.0} = 0 \\ \text{tsa.0.1.Def: } & \text{sscfu.0.AB1} + \text{sscfu.0.C1} - \text{tsa.0.1} = 0 \\ \text{tsa.0.2.Def: } & \text{sscfu.0.B2} - \text{tsa.0.2} = 0 \\ \text{tsa.0.3.Def: } & \text{sscfu.0.BC1} + \text{sscfu.0.C2} - \text{tsa.0.3} = 0 \\ \text{tsa.0.4.Def: } & \text{sscfu.0.AB2} - \text{tsa.0.4} = 0 \\ \text{tsa.0.5.Def: } & \text{sscfu.0.BALL1} - \text{tsa.0.5} = 0 \\ \text{tsa.0.6.Def: } & \text{sscfu.0.BC2} - \text{tsa.0.6} = 0 \\ \text{tsa.0.7.Def: } & \text{sscfu.0.BALL2} - \text{tsa.0.7} = 0 \\ \text{tsa.0.POOL.Def: } & \text{sscfu.0.POOL} - \text{tsa.0.POOL} = 0 \\ \text{tsa.1.0.Def: } & \text{sscfu.1.A1} + \text{sscfu.1.A2} + \text{sscfu.1.B1} - \text{tsa.1.0} = 0 \\ \text{tsa.1.1.Def: } & \text{sscfu.1.AB1} + \text{sscfu.1.C1} - \text{tsa.1.1} = 0 \\ \text{tsa.1.2.Def: } & \text{sscfu.1.B2} - \text{tsa.1.2} = 0 \\ \text{tsa.1.3.Def: } & \text{sscfu.1.BC1} + \text{sscfu.1.C2} - \text{tsa.1.3} = 0 \\ \text{tsa.1.4.Def: } & \text{sscfu.1.AB2} - \text{tsa.1.4} = 0 \\ \text{tsa.1.5.Def: } & \text{sscfu.1.BALL1} - \text{tsa.1.5} = 0 \\ \text{tsa.1.6.Def: } & \text{sscfu.1.BC2} - \text{tsa.1.6} = 0 \\ \text{tsa.1.7.Def: } & \text{sscfu.1.BALL2} - \text{tsa.1.7} = 0 \\ \text{tsa.1.POOL.Def: } & -\text{tsa.1.POOL} + \text{sscfu.1.POOL} = 0 \end{aligned}$$

$$\begin{aligned}
& \text{tsa.2.0.Def: } \text{sscfu.2.A1} + \text{sscfu.2.A2} + \text{sscfu.2.B1} - \text{tsa.2.0} = 0 \\
& \text{tsa.2.1.Def: } \text{sscfu.2.AB1} + \text{sscfu.2.C1} - \text{tsa.2.1} = 0 \\
& \text{tsa.2.2.Def: } \text{sscfu.2.B2} - \text{tsa.2.2} = 0 \\
& \text{tsa.2.3.Def: } \text{sscfu.2.BC1} + \text{sscfu.2.C2} - \text{tsa.2.3} = 0 \\
5 \quad & \text{tsa.2.4.Def: } \text{sscfu.2.AB2} - \text{tsa.2.4} = 0 \\
& \text{tsa.2.5.Def: } \text{sscfu.2.BALL1} - \text{tsa.2.5} = 0 \\
& \text{tsa.2.6.Def: } \text{sscfu.2.BC2} - \text{tsa.2.6} = 0 \\
& \text{tsa.2.7.Def: } \text{sscfu.2.BALL2} - \text{tsa.2.7} = 0 \\
& \text{tsa.2.POOL.Def: } \text{sscfu.2.POOL} - \text{tsa.2.POOL} = 0 \\
10 \quad & \text{tsa.3.0.Def: } \text{sscfu.3.A1} + \text{sscfu.3.A2} + \text{sscfu.3.B1} - \text{tsa.3.0} = 0 \\
& \text{tsa.3.1.Def: } \text{sscfu.3.AB1} + \text{sscfu.3.C1} - \text{tsa.3.1} = 0 \\
& \text{tsa.3.2.Def: } \text{sscfu.3.B2} - \text{tsa.3.2} = 0 \\
& \text{tsa.3.3.Def: } \text{sscfu.3.BC1} + \text{sscfu.3.C2} - \text{tsa.3.3} = 0 \\
& \text{tsa.3.4.Def: } \text{sscfu.3.AB2} - \text{tsa.3.4} = 0 \\
15 \quad & \text{tsa.3.5.Def: } \text{sscfu.3.BALL1} - \text{tsa.3.5} = 0 \\
& \text{tsa.3.6.Def: } \text{sscfu.3.BC2} - \text{tsa.3.6} = 0 \\
& \text{tsa.3.7.Def: } \text{sscfu.3.BALL2} - \text{tsa.3.7} = 0 \\
& \text{tsa.3.POOL.Def: } \text{sscfu.3.POOL} - \text{tsa.3.POOL} = 0
\end{aligned}$$

In step 350, the upgraded function space constraint tsu.DP.TST.Def is determined. The upgraded function space constraint ensures that upgrades for function space are given in an efficient manner (e.g., when a choice of a smaller room and a larger room is available for an upgrade, a smaller room is assigned to a group who needs the smaller room and a larger room is assigned to a group who needs the larger room). The upgraded function space is defined as:

$$\begin{aligned}
25 \quad & \text{tsu.DP.TST.Def:} \\
& \sum_{\text{OID}} N(\text{OID}, \text{DP}, \text{TST}) w_{\text{Opp.OID}} + \sum_{\text{RTST} | \text{ATST} = \text{TST}} \text{upg.DP.RTST.ATST} - \sum_{\text{ATST} | \text{RTST} = \text{TST}} \text{upg.DP.RTST.ATST} - \text{tsa.DP.TST} \leq 0
\end{aligned}$$

Or written another way:

$$\begin{aligned}
30 \quad & \sum_{\text{OID}} N(\text{OID}, \text{DP}, \text{TST}) w_{\text{Opp.OID}} + \sum_{\text{RTST} | \text{ATST} = \text{TST}} \text{upg.DP.RTST.ATST} - \sum_{\text{ATST} | \text{RTST} = \text{TST}} \text{upg.DP.RTST.ATST} \leq \text{tsa.DP.TST}
\end{aligned}$$

$N(\text{OID}, \text{DP}, \text{TST})$  represents the number of target spaces of target space type (TST) demanded by opportunity ID (OID) during day part (DP).  $w_{\text{Opp.OID}}$

represents whether an opportunity is accepted or turned down (There are NOID such variables, where NOID is the number of opportunities.) tsa.DP.TST represents the target space available of a given target space type (i.e., function space category). upg.DP.RTST.ATST represents the upgrades from the requested target space type to the assigned target space type. RTST represents the requested target space type and ATST represents the assigned target space type.

DP is the day part and is 0, 1, 2, or 3 (each representing 6 hours, as explained above). TST is the target space type (space category) from Table 9. OID is the opportunity ID from Table 11. Thus:

- 10      tsu.0.0.Def: - upg.0.0.1 - tsa.0.0  $\leq$  0  
          tsu.0.1.Def: upg.0.0.1 - upg.0.1.2 - tsa.0.1  $\leq$  0  
          tsu.0.2.Def: upg.0.1.2 - upg.0.2.3 - tsa.0.2  $\leq$  0  
          tsu.0.3.Def: upg.0.2.3 - upg.0.3.4 - tsa.0.3  $\leq$  0  
          tsu.0.4.Def: upg.0.3.4 - upg.0.4.5 - tsa.0.4  $\leq$  0  
 15      tsu.0.5.Def: upg.0.4.5 - upg.0.5.6 - tsa.0.5  $\leq$  0  
          tsu.0.6.Def: upg.0.5.6 - upg.0.6.7 - tsa.0.6  $\leq$  0  
          tsu.0.7.Def: upg.0.6.7 - tsa.0.7  $\leq$  0  
          tsu.0.POOL.Def: wOpp.IBM - tsa.0.POOL  $\leq$  0  
  
          tsu.1.0.Def: - upg.1.0.1 - tsa.1.0  $\leq$  0  
 20      tsu.1.1.Def: upg.1.0.1 - upg.1.1.2 - tsa.1.1  $\leq$  0  
          tsu.1.2.Def: upg.1.1.2 - upg.1.2.3 - tsa.1.2  $\leq$  0  
          tsu.1.3.Def: wOpp.ATT + upg.1.2.3 - upg.1.3.4 - tsa.1.3  $\leq$  0  
          tsu.1.4.Def: upg.1.3.4 - upg.1.4.5 - tsa.1.4  $\leq$  0  
          tsu.1.5.Def: upg.1.4.5 - upg.1.5.6 - tsa.1.5  $\leq$  0  
 25      tsu.1.6.Def: upg.1.5.6 - upg.1.6.7 - tsa.1.6  $\leq$  0  
          tsu.1.7.Def: upg.1.6.7 - tsa.1.7  $\leq$  0  
          tsu.1.POOL.Def: - tsa.1.POOL  $\leq$  0  
  
          tsu.2.0.Def: - upg.2.0.1 - tsa.2.0  $\leq$  0  
          tsu.2.1.Def: upg.2.0.1 - upg.2.1.2 - tsa.2.1  $\leq$  0  
 30      tsu.2.2.Def: wOpp.CSCO + wOpp.IBM + upg.2.1.2 - upg.2.2.3 - tsa.2.2  $\leq$  0  
          tsu.2.3.Def: wOpp.ATT + upg.2.2.3 - upg.2.3.4 - tsa.2.3  $\leq$  0  
          tsu.2.4.Def: upg.2.3.4 - upg.2.4.5 - tsa.2.4  $\leq$  0  
          tsu.2.5.Def: upg.2.4.5 - upg.2.5.6 - tsa.2.5  $\leq$  0  
          tsu.2.6.Def: upg.2.5.6 - upg.2.6.7 - tsa.2.6  $\leq$  0  
 35      tsu.2.7.Def: upg.2.6.7 - tsa.2.7  $\leq$  0  
          tsu.2.POOL.Def: - tsa.2.POOL  $\leq$  0

tsu.3.0.Def:  $- \text{upg.3.0.1} - \text{tsa.3.0} \leq 0$   
tsu.3.1.Def:  $\text{upg.3.0.1} - \text{upg.3.1.2} - \text{tsa.3.1} \leq 0$   
tsu.3.2.Def:  $\text{upg.3.1.2} - \text{upg.3.2.3} - \text{tsa.3.2} \leq 0$   
tsu.3.3.Def:  $\text{upg.3.2.3} - \text{upg.3.3.4} - \text{tsa.3.3} \leq 0$   
5 tsu.3.4.Def:  $\text{upg.3.3.4} - \text{upg.3.4.5} - \text{tsa.3.4} \leq 0$   
tsu.3.5.Def:  $\text{upg.3.4.5} - \text{upg.3.5.6} - \text{tsa.3.5} \leq 0$   
tsu.3.6.Def:  $\text{upg.3.5.6} - \text{upg.3.6.7} - \text{tsa.3.6} \leq 0$   
tsu.3.7.Def:  $\text{upg.3.6.7} - \text{tsa.3.7} \leq 0$   
tsu.3.POOL:  $- \text{tsa.3.POOL} \leq 0$

## 10 **Determine Bounds**

Figure 4 is a flowchart illustrating various bounds and how the various bounds are determined. In step 405, the bound for the amount of transient rooms accepted is set.

$$0 \leq x.AD(i).LS(i).RC(i).RT(i)$$

15 Thus, for example:

$$\begin{aligned} 0 &\leq x.0.2.0.0 \\ 0 &\leq x.1.0.0.1 \\ 0 &\leq x.2.0.0.1 \\ 0 &\leq x.2.0.0.2 \end{aligned}$$

20 In step 410, the bound for the amount of transient rooms assigned is set.

$$0 \leq y.AD(i).LS(i).RC(i).RT(i).ART$$

Thus, for example:

$$\begin{aligned} 0 &\leq y.0.2.0.0.0 \\ 0 &\leq y.0.2.0.0.1 \\ 25 \quad 0 &\leq y.0.2.0.0.2 \\ 0 &\leq y.1.0.0.1.1 \\ 0 &\leq y.1.0.0.1.2 \\ 0 &\leq y.2.0.0.1.1 \\ 0 &\leq y.2.0.0.1.2 \\ 30 \quad 0 &\leq y.2.0.0.2.2 \end{aligned}$$

In step 415, the bound for the amount of assigned group rooms is set.

$$0 \leq \text{yOpp.OID.SD.RT.ART}$$

Thus, for example:

$$\begin{array}{ll}
 & 0 \leq \text{yOpp.ATT.0.0.0} \\
 & 0 \leq \text{yOpp.CSCO.0.0.0} \\
 5 & 0 \leq \text{yOpp.IBM.0.0.0} \\
 & 0 \leq \text{yOpp.ATT.0.0.1} \\
 & 0 \leq \text{yOpp.CSCO.0.0.1} \\
 & 0 \leq \text{yOpp.IBM.0.0.1} \\
 & 0 \leq \text{yOpp.ATT.0.0.2} \\
 10 & 0 \leq \text{yOpp.CSCO.0.0.2} \\
 & 0 \leq \text{yOpp.IBM.0.0.2} \\
 & 0 \leq \text{yOpp.ATT.1.1.1} \\
 & 0 \leq \text{yOpp.IBM.1.1.1} \\
 & 0 \leq \text{yOpp.ATT.1.1.2} \\
 15 & 0 \leq \text{yOpp.IBM.1.1.2}
 \end{array}$$

In step 420, the bounds for the wOpp.OID are set. In this case the value for wOpp.OID is either 0 or 1:

$$0 \leq \text{wOpp.OID} \leq 1$$

Thus, for example:

$$\begin{array}{ll}
 20 & 0 \leq \text{wOpp.ATT} \leq 1 \\
 & 0 \leq \text{wOpp.CSCO} \leq 1 \\
 & 0 \leq \text{wOpp.IBM} \leq 1
 \end{array}$$

In step 425, the bounds for sscfu.DP.SS are set. sscfu.DP.SS is either 0 or

$$25 \quad 1.$$

$$0 \leq \text{sscfu.DP.SS} \leq 1$$

Thus, for example:

$$\begin{array}{ll}
 & 0 \leq \text{sscfu.0.A1} \leq 1 \\
 & 0 \leq \text{sscfu.0.AB1} \leq 1 \\
 30 & 0 \leq \text{sscfu.0.BALL1} \leq 1 \\
 & 0 \leq \text{sscfu.0.A2} \leq 1 \\
 & 0 \leq \text{sscfu.0.AB2} \leq 1 \\
 & 0 \leq \text{sscfu.0.BALL2} \leq 1 \\
 & 0 \leq \text{sscfu.0.B1} \leq 1 \\
 35 & 0 \leq \text{sscfu.0.BC1} \leq 1 \\
 & 0 \leq \text{sscfu.0.B2} \leq 1
 \end{array}$$

	$0 \leq \text{sscfu}.0.\text{BC2} \leq 1$
	$0 \leq \text{sscfu}.0.\text{C1} \leq 1$
	$0 \leq \text{sscfu}.0.\text{C2} \leq 1$
	$0 \leq \text{sscfu}.0.\text{POOL} \leq 1$
5	$0 \leq \text{sscfu}.1.\text{A1} \leq 1$
	$0 \leq \text{sscfu}.1.\text{AB1} \leq 1$
	$0 \leq \text{sscfu}.1.\text{BALL1} \leq 1$
	$0 \leq \text{sscfu}.1.\text{A2} \leq 1$
	$0 \leq \text{sscfu}.1.\text{AB2} \leq 1$
10	$0 \leq \text{sscfu}.1.\text{BALL2} \leq 1$
	$0 \leq \text{sscfu}.1.\text{B1} \leq 1$
	$0 \leq \text{sscfu}.1.\text{BC1} \leq 1$
	$0 \leq \text{sscfu}.1.\text{B2} \leq 1$
	$0 \leq \text{sscfu}.1.\text{BC2} \leq 1$
15	$0 \leq \text{sscfu}.1.\text{C1} \leq 1$
	$0 \leq \text{sscfu}.1.\text{C2} \leq 1$
	$0 \leq \text{sscfu}.1.\text{POOL} \leq 1$
	$0 \leq \text{sscfu}.2.\text{A1} \leq 1$
	$0 \leq \text{sscfu}.2.\text{AB1} \leq 1$
20	$0 \leq \text{sscfu}.2.\text{BALL1} \leq 1$
	$0 \leq \text{sscfu}.2.\text{A2} \leq 1$
	$0 \leq \text{sscfu}.2.\text{AB2} \leq 1$
	$0 \leq \text{sscfu}.2.\text{BALL2} \leq 1$
	$0 \leq \text{sscfu}.2.\text{B1} \leq 1$
25	$0 \leq \text{sscfu}.2.\text{BC1} \leq 1$
	$0 \leq \text{sscfu}.2.\text{B2} \leq 1$
	$0 \leq \text{sscfu}.2.\text{BC2} \leq 1$
	$0 \leq \text{sscfu}.2.\text{C1} \leq 1$
	$0 \leq \text{sscfu}.2.\text{C2} \leq 1$
30	$0 \leq \text{sscfu}.2.\text{POOL} \leq 1$
	$0 \leq \text{sscfu}.3.\text{A1} \leq 1$
	$0 \leq \text{sscfu}.3.\text{AB1} \leq 1$
	$0 \leq \text{sscfu}.3.\text{BALL1} \leq 1$
	$0 \leq \text{sscfu}.3.\text{A2} \leq 1$
35	$0 \leq \text{sscfu}.3.\text{AB2} \leq 1$
	$0 \leq \text{sscfu}.3.\text{BALL2} \leq 1$
	$0 \leq \text{sscfu}.3.\text{B1} \leq 1$
	$0 \leq \text{sscfu}.3.\text{BC1} \leq 1$
	$0 \leq \text{sscfu}.3.\text{B2} \leq 1$
40	$0 \leq \text{sscfu}.3.\text{BC2} \leq 1$
	$0 \leq \text{sscfu}.3.\text{C1} \leq 1$
	$0 \leq \text{sscfu}.3.\text{C2} \leq 1$
	$0 \leq \text{sscfu}.3.\text{POOL} \leq 1$

In step 430, the bounds for the room protection are set:  $0 \leq \text{Rm}(\text{SD}, \text{Rt})$

45            Thus, for example:



0 ≤ RmPr.0.0 ≤ 21  
0 ≤ RmPr.0.1 ≤ 22  
0 ≤ RmPr.1.0 ≤ 23  
0 ≤ RmPr.1.1 ≤ 24  
5 0 ≤ RmPr.2.0 ≤ 25  
0 ≤ RmPr.2.1 ≤ 26

## **Conclusion**

While various embodiments of the present invention have been described above, it should be understood that they have been presented by way of example, and not limitation. It will be apparent to persons skilled in the relevant art(s) that various changes in form and detail can be made therein without departing from the spirit and scope of the present invention. Thus, the present invention should not be limited by any of the above-described exemplary embodiments, but should be defined only in accordance with the following claims and their equivalents.

15 In addition, it should be understood that the Figures and Tables illustrated in the attachments, which highlight the functionality and advantages of the present invention, are presented for example purposes only. The architecture of the present invention is sufficiently flexible and configurable, such that it may be utilized (and navigated) in ways other than that shown in the accompanying Figures.

20 Further, the purpose of the Abstract is to enable the U.S. Patent and Trademark Office and the public generally, and especially the scientists, engineers and practitioners in the art who are not familiar with patent or legal terms or phraseology, to determine quickly from a cursory inspection the nature and essence of the technical disclosure of the application. The Abstract is not intended to be limiting as to the scope of the present invention in any way.

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Table 1: Description of Subscripts

Subscript	Description
AD	Arrival Date
LS	Length of Stay
RC	Rate Category
RT	Room Type
ART	Assigned Room Type
TRT	Target Room Type
DP	Day Part
OID	Opportunity ID
SSN	Source Space Name
TST	Target Space Type
SS	Specific Space
SD	Stay Date

Table 2: Number and Types of Variables

Variable	Number	Type
$x.AD(i).LS(i).RC(i).RT(i)$	$I$	Continuous
$y.AD(i).LS(i).RC(i).RT(i).ART$	$\sum_i (NRT - RT(i) + 1)$	Continuous
$TrRev$	$1$	Continuous
$UpCst$	$1$	Continuous
$GrRev$	$1$	Continuous
$yOpp.OID.SD.RT.ART$	$\sum_{OID,SD,RT   N(OID,SD,RT) > 0} (NRT - RT)$	Continuous
$RmPr.SD.RT$	$NSD \times NRT$	Continuous
$sscfu.DP.SS$	$NDP \times NSS$	Binary
$tsa.DP.TST$	$NDP \times NTST$	Continuous
$wOpp.OID$	$NOID$	Binary
$upg.DP.RTST.ATST$	$NTST - 1$	Continuous

Table 3: Number of Constraints

Constraint	Number
$xUbCon.i$	$I$
$trUpg.AD(i).LS(i).RC(i).RT(i)$	$I$
$TrRevDef$	1
$UpCstDef$	1
$RmPr.SD.RT.Def$	$NSD \times NRT$
$GpRmPr.OID.SD.RT.Def$	$\sum_{OID,SD,RT/N(OID,SD,RT)>0} 1$
$GrRevDef$	1
$spc.DP.SS.Def$	$NDP \times NSS$
$tsa.DP.TST.Def$	$NDP \times NTST$
$tsu.DP.TST.Def$	$NDP \times NTST$

Table 4: Parameters

Arr. Dates	Rate Cat.	Rm Types	LOS	Prop Code	Post Date	Brand	Rate Cat.
3	1	3	3	HOTEL	37718	FS	A

Table 5: Supply Information

Room Type (RT)	Stay Date (SD)	Rooms (Number of Rooms Available)
0	0	20
1	0	20
2	0	20
0	1	20
1	1	19
2	1	20
0	2	20
1	2	20
2	2	18

Table 6: Transient Demand Information

Demand (i)	Arrival Date (AD)	Length of Stay (LS)	Rate Category (RC)	Room Type (RT)	Number of Rooms Requested [N(i)]	Rate
1	0	2	0	0	3	100
2	1	0	0	1	4	100
3	2	0	1	1	5	120
4	2	0	2	2	6	150

Table 7: Target Space Information

Property Code	Target Space Type	Area
HOTEL	0	100
HOTEL	1	200
HOTEL	2	250
HOTEL	3	300
HOTEL	4	350
HOTEL	5	400
HOTEL	6	550
HOTEL	7	650
HOTEL	POOL	1000

Table 8: Function Space Upgrade Information

Property Code	Upgraded Target Space Type	Requested Target Space Type
HOTEL	1	0
HOTEL	2	1
HOTEL	3	2
HOTEL	4	3
HOTEL	5	4
HOTEL	6	5
HOTEL	7	6

Table 9: Function Space Category Information

Space Code	Space Category (Target Space Type)	Space Type	Area (sq. ft.)
A1	0	FRM	100
A2	0	FRM	100
AB1	1	FRM	200
AB2	4	FRM	350
B1	0	FRM	100
B2	2	FRM	250
BALL1	5	FRM	400
BALL2	7	FRM	650
BC1	3	FRM	300
BC2	6	FRM	550
C1	1	FRM	200
C2	3	FRM	300
POOL	POOL	ALT	1000

Table 10: Function Space Structure Information

Property Code	Indivisible Space Code	Configured Space Codes
HOTEL	A1	AB1 BALL1
HOTEL	A2	AB2 BALL2
HOTEL	B1	AB1 BALL1 BC1
HOTEL	B2	AB2 BALL2 BC2
HOTEL	C1	BALL1 BC1
HOTEL	C2	BALL2 BC2

Table 11: Opportunity Information

Property Code	Opportunity ID	Revenue	Profit	Is Actual	Is StayThru
HOTEL	IBM	2000	1053	1	0
HOTEL	ATT	2001	1052	1	0
HOTEL	CSCO	2002	1051	0	0

Table 12: Opportunity Sleeping Demand Information

Property Code	Opportunity ID	Room Type	Stay Date	Demand
HOTEL	IBM	0	0	3
HOTEL	IBM	1	1	7
HOTEL	ATT	0	0	4
HOTEL	ATT	1	1	8
HOTEL	CSCO	0	0	5

Table 13: Opportunity Function Space Demand

Prop Code	Opp ID	Tgt Space Type	St. Day	St. Hr	End Day	End Hr	Demand
HOTEL	IBM	POOL	0	8	0	9	1
HOTEL	ATT	3	0	13	0	15	1
HOTEL	CSCO	2	0	14	0	16	1
HOTEL	IBM	2	0	14	0	16	1